

1. Use notations with care such as

$$\begin{array}{l} \in \\ \subset \text{ (or } \subseteq) \end{array}$$

2. Sentence should as "If, then", or "..... holds for each (or all)"

If he is a CU student then he is good
若天氣好, 我去打波.

$$P \Rightarrow Q$$

If $x \in C$ then $x \in G$

$x \in G$, for all $x \in C$

$$(C \subseteq G).$$

3. Negations of sentences in the Question 2 above.

4. Using axioms I and II, you can show many familiar rules/formulae that you learnt in schools such that

uniqueness of zero, one, "inverse" of x with respect to addition or multiplication, cancellation laws,

$$(a+b)^2 = a^2 + 2ab + b^2,$$

where $a^2 := a \cdot a$ and $2x := x + x \quad \forall a, x \in \mathbb{R}.$

5*. The natural numbers and (Generalized) Mathematical Induction and

$$1 < 2 < 3 < 4 < 5 \dots\dots$$

and there does not exist a nature number strictly between a natural number n and $n+1$.

6*. Given a set A of real numbers and a real number u , define " u is an upper bound of A " and its negation (namely what is meant that " u is not an upper bound of A " (in doing so NO Negative term is allowed to be employed!). Give the definition of "largest element of A ". Give an example showing that an upper bound of A may not be an element of A and that a set A need not have the largest element.

7. Do Question 6 but for lower bounds, smallest elements etc.

8*. Given a lower bound c for a nonempty set B of real numbers define " c is a (=the) greatest lower bound for B " and its negation.

(hand-in your solutions of questions with *; not yet set deadline: to be announced a a later date)